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# The Constrained $E_6$ SSM at the LHC

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1<sup>st</sup> September 2011

Based on:

P. Athron, S.F. King, DJM, S. Moretti, R. Nevzorov

arXiv:1102.4363, arXiv:0904.2169, arXiv:0901.1192

[S.F.King, S.Moretti & R. Nevzorov, Phys.Rev. D73 (2006) 035009 ; Phys.Lett. B634 (2006) 278-284]

“Inspired” by the gauge group  $E_6$ , breaking to the SM via

$$\begin{aligned} E_6 &\rightarrow SO(10) \times U(1)_\psi \\ &\quad \downarrow \\ &\quad SU(5) \times U(1)_\chi \\ &\quad \quad \downarrow \\ &\quad \quad SU(3)_C \times SU(2)_W \times U(1)_Y \end{aligned}$$

where only one linear superposition of the extra  $U(1)$  symmetries survives to low energies:

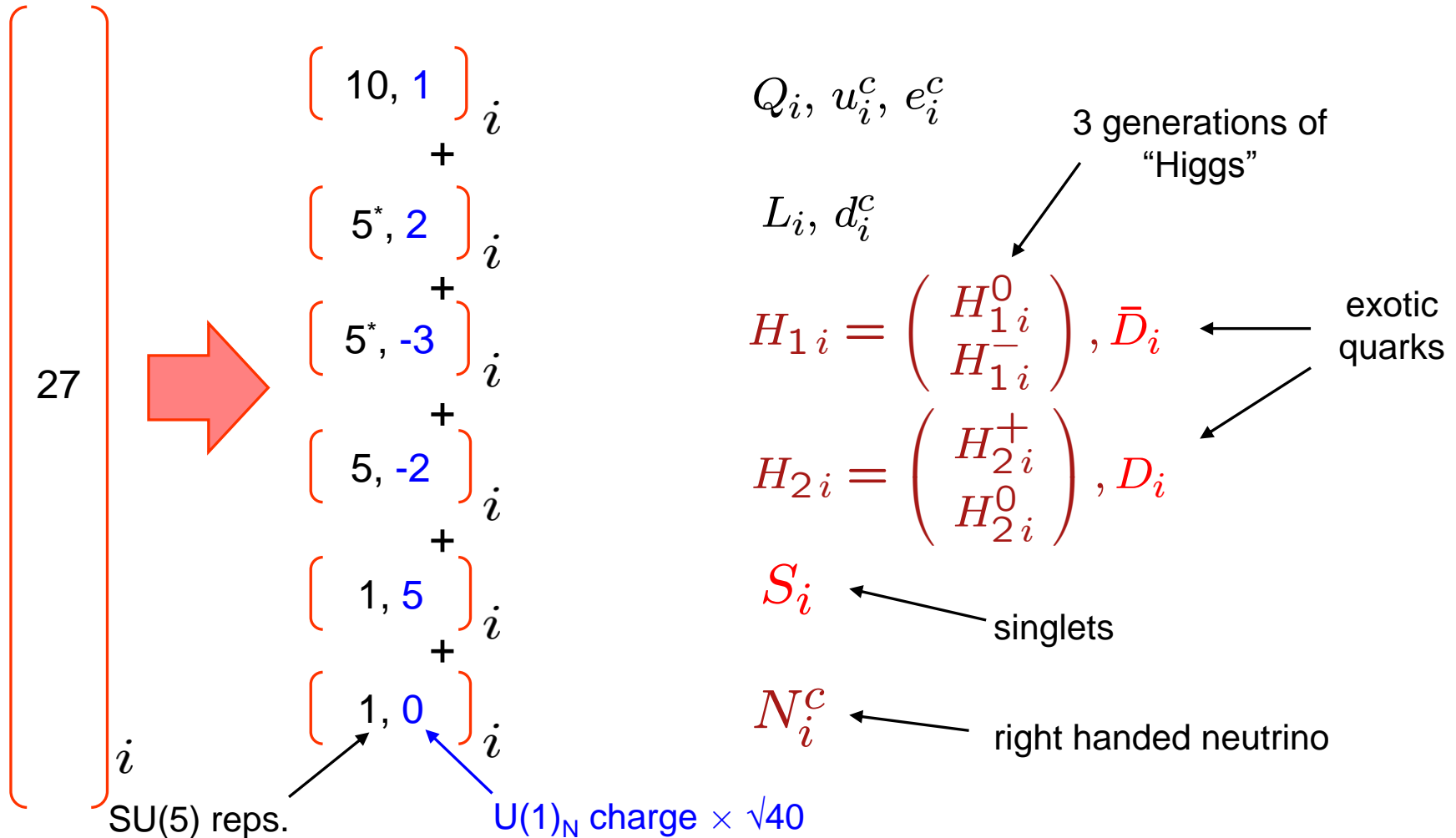
$$U(1)_N = \frac{1}{4}U(1)_\chi + \frac{\sqrt{15}}{4}U(1)_\psi$$

This combination is required in order to keep the right handed neutrinos sterile.

So the  $E_6$ SSM is really a  $SU(3)_C \times SU(2)_W \times U(1)_Y \times U(1)_N$  gauge theory.

# Matter Content

All the SM matter fields are contained in one 27-plet of  $E_6$  per generation.



- Only the third generation Higgs boson gains a VEV.  
The others are neutral and charged scalars - we call them “**inert Higgs**”.  
Three generations of singlets, with  $\langle S_3 \rangle \neq 0$
- Extra  $U(1) \rightarrow$  extra gauge boson,  $Z'$ .  
After EWSB this will become massive (after eating the imaginary part of  $S_3$ )
- Additional  $SU(2)$  doublets  $H'$  and  $\bar{H}'$ , relics of an additional  $27'$  and  $\bar{27}'$  which survive down to low energies, and are required for gauge unification.
- $Z_2^B$  or  $Z_2^L$  symmetries to prevent proton decay (analogous to R-parity in the MSSM)  
 $Z_2^B \rightarrow D$  is a **leptoquark**                       $Z_2^L \rightarrow D$  is a **diquark**
- Approximate  $Z_2^H$  symmetry to evade large **Flavour Changing Neutral Currents**  
3<sup>rd</sup> generation Higgs and singlet superfields even, all other fields odd.  
Must only be approximate to allow exotic particles to decay.

# The Constrained E6SSM

The E<sub>6</sub>SSM has 43 new parameters compared with the MSSM (14 are phases).

But if we apply constraints at the GUT scale, this is drastically reduced.

Set: 
$$g_1(M_X) = g_2(M_X) = g_3(M_X) = g'_1(M_X)$$

soft scalar masses  $\longrightarrow m_0$

gaugino masses  $\longrightarrow M_{1/2}$

$$A_{\lambda_i}(M_X) = A_{\kappa_i}(M_X) = A_{t,b,\tau}(M_X) = A(M_X)$$

Important parameters:  $\lambda_i, \kappa_i, h_t, h_b, h_\tau, m_0, M_{1/2}, A$

We derived Renormalisation Group Equations, and modified SoftSuSY [Allanach, arXiv:hep-ph/0104145] to run down the GUT scale parameters to low energies.

- Gauge and Yukawa couplings (2 loop),
- Soft breaking gaugino and trilinear masses (2 loop),
- Soft scalar masses (1 loop).

For most allowed scenarios  $m_0 \gtrsim M_{1/2}$ , so squarks tend to be heavier than the gluino

Neutralinos, charginos and gluino

$$m_{\tilde{\chi}_1^0} \approx M_1 \quad m_{\tilde{g}} \approx M_3$$

$$m_{\tilde{\chi}_2^0} \approx m_{\tilde{\chi}_1^\pm} \approx M_2$$

$$m_{\tilde{\chi}_{3,4}^0} \approx m_{\tilde{\chi}_2^\pm} \approx \mu = \lambda \langle S \rangle$$

$$m_{\tilde{\chi}_{5,6}^0} \approx M_{Z'}$$

Higgs bosons

$$m_{h_1} \approx M_Z + \Delta$$

$$m_{h_2} \approx m_{H^\pm} \approx m_A$$

$$m_{h_3} \approx M_{Z'}$$

$$\text{exotic quarks} \approx \kappa_i \langle S \rangle$$

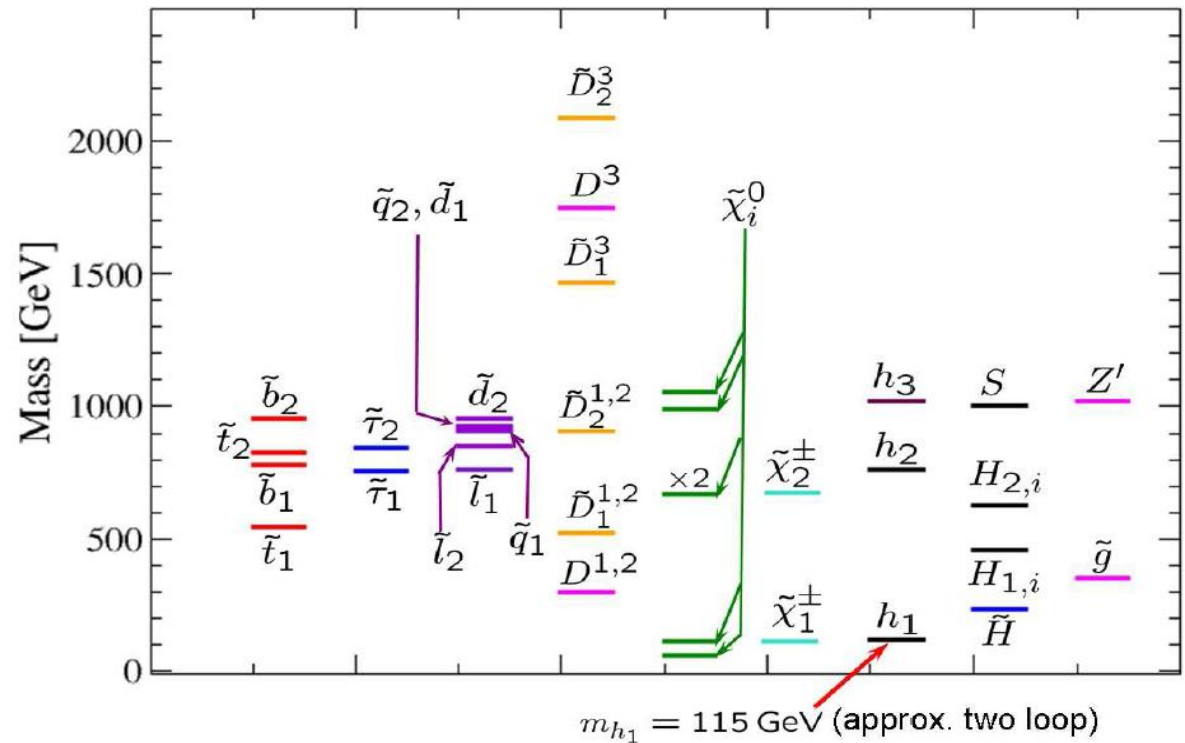
$$\text{exotic squarks} \approx m_{D_i}^2 + \kappa_i^2 \langle S \rangle^2 \quad + \text{mixing and auxiliary D-terms}$$

$$\text{inert Higgs} \approx m_{H_i}^2 + \lambda_i^2 \langle S \rangle^2 \quad + \text{auxiliary D-terms}$$

$$\text{inert higgsino} \approx \lambda_i \langle S \rangle$$

# “Early Discovery” Benchmark C

$$\begin{aligned}
 \tan \beta &= 10 \\
 \lambda_3(M_X) &= -0.378 \\
 \lambda_{1,2}(M_X) &= 0.1 \\
 \kappa_3(M_X) &= 0.42 \\
 \kappa_{1,2}(M_X) &= 0.06 \\
 \sqrt{2}\langle S \rangle &= 2.7 \text{ TeV} \\
 M_{1/2} &= 388 \text{ GeV} \\
 m_0 &= 681 \text{ GeV} \\
 A_0 &= 645 \text{ GeV}
 \end{aligned}$$

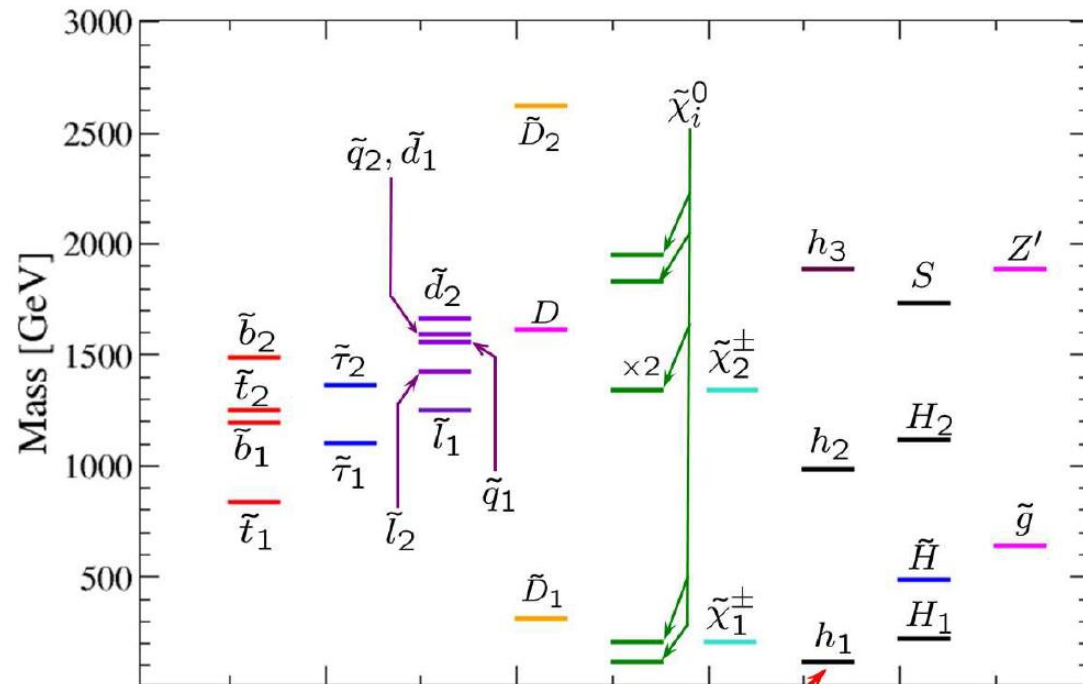


- $\kappa_1 = \kappa_2 \neq \kappa_3$  so degeneracy of Ds is lifted.
- lightest exotic quark is 300 GeV



# “Late Discovery” Benchmark 4

$$\begin{aligned}
 \tan \beta &= 30 \\
 \lambda_3(M_X) &= -0.3847 \\
 \lambda_{1,2}(M_X) &= 0.1 \\
 \kappa_{1,2,3}(M_X) &= 0.1579 \\
 \sqrt{2}\langle S \rangle &= 5 \text{ TeV} \\
 M_{1/2} &= 725 \text{ GeV} \\
 m_0 &= 1074 \text{ GeV} \\
 A_0 &= 1726 \text{ GeV}
 \end{aligned}$$



$m_{h_1} = 114 \text{ GeV}$  (approx. two loop)

- $\kappa_1 = \kappa_2 = \kappa_3$  so Ds are degenerate (1612 GeV)
- lightest exotic squark is 312 GeV (due to large mixing)



The  $U(1)_N$   $Z'$  has two differences compared to the sequential  $Z'$ :

- The couplings are given by the  $U(1)_N$  charges, so different to those of the SM Z-boson
- The  $Z'$  may decay to exotic matter, altering the width and Branching Ratios

$Z'_N$ partial width [GeV]	BMC	BM4
$\Gamma(Z'_N \rightarrow l^+ l^-)$ ( $l = e, \mu$ or $\tau$ )	0.41	0.77
$\Sigma_l \Gamma(Z'_N \rightarrow \nu_l \bar{\nu}_l)$ (all neutrinos)	0.87	1.64
$\Sigma_l \Gamma(Z'_N \rightarrow l^+ l^-, \nu_l \bar{\nu}_l)$ (all leptons)	2.10	3.96
$\Sigma_q \Gamma(Z'_N \rightarrow q \bar{q})$ (all quarks)	5.31	10.08
$\Sigma_i \Gamma(Z'_N \rightarrow D_i \bar{D}_i)$ (exotic fermions)	3.49	0.00
$\Sigma_\alpha \Gamma(Z'_N \rightarrow \tilde{H}_\alpha \tilde{H}_\alpha)$ (inert Higgsinos)	3.09	5.19
$\Sigma_\alpha \Gamma(Z'_N \rightarrow \tilde{S}_\alpha \tilde{S}_\alpha)$ (singlinos)	4.05	7.63
$\Sigma_i \Gamma(Z'_N \rightarrow \tilde{D}_i \tilde{D}_i)$ (exotic scalars)	0.00	0.19
$\Sigma_f \Gamma(Z'_N \rightarrow \tilde{f} \tilde{f})$ (sfermions)	0.00	0.010
$\Sigma_\alpha \Gamma(Z'_N \rightarrow H_\alpha H_\alpha)$ (inert Higgses)	0.026	0.39
$\Sigma_j \Gamma(Z'_N \rightarrow \tilde{\chi}_j \tilde{\chi}_j)$ (gauginos)	$6.50 \times 10^{-4}$	$7.92 \times 10^{-5}$
$\Gamma_{\text{tot}}$ (all)	18.07	27.45

Example Decay:

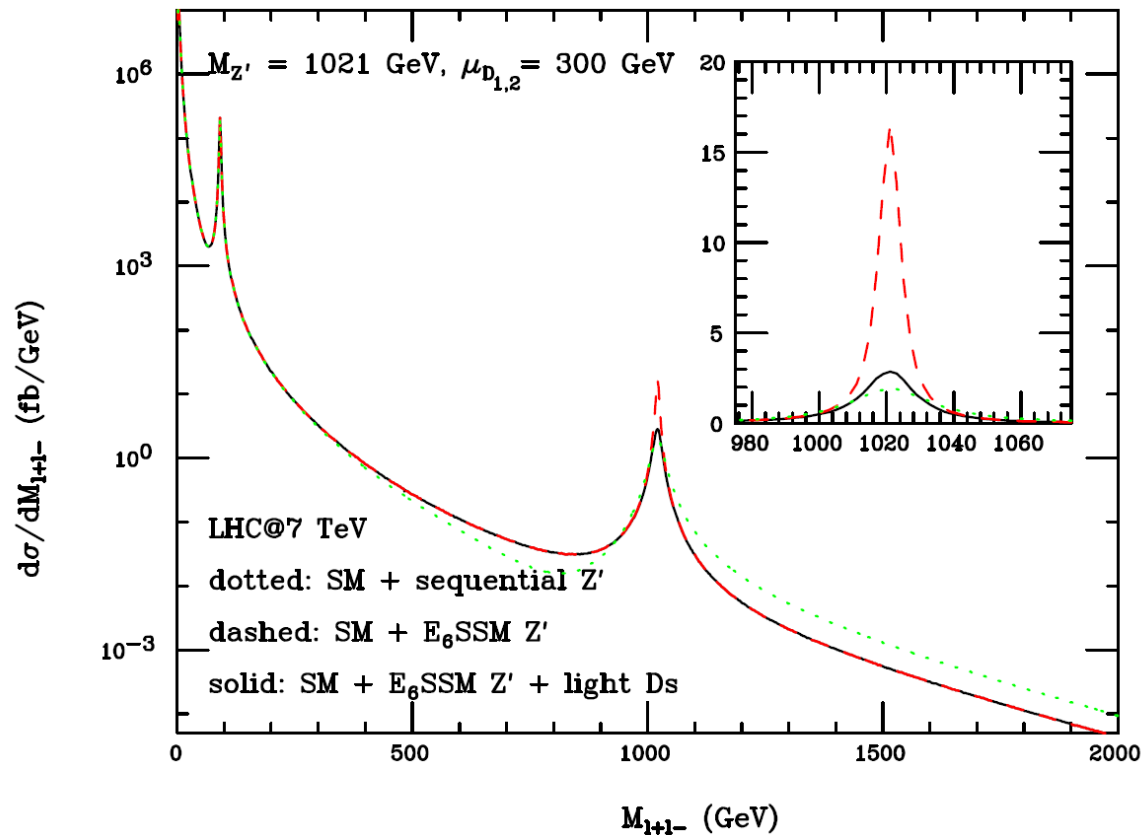
$$Z' \rightarrow \tilde{S}_2 \tilde{S}_2$$

$\left\{ \begin{array}{l} \rightarrow \\ \rightarrow \end{array} \right.$

$\tilde{f} \tilde{f} \tilde{S}_1$   
 $\tilde{f} \tilde{f} \tilde{S}_1$

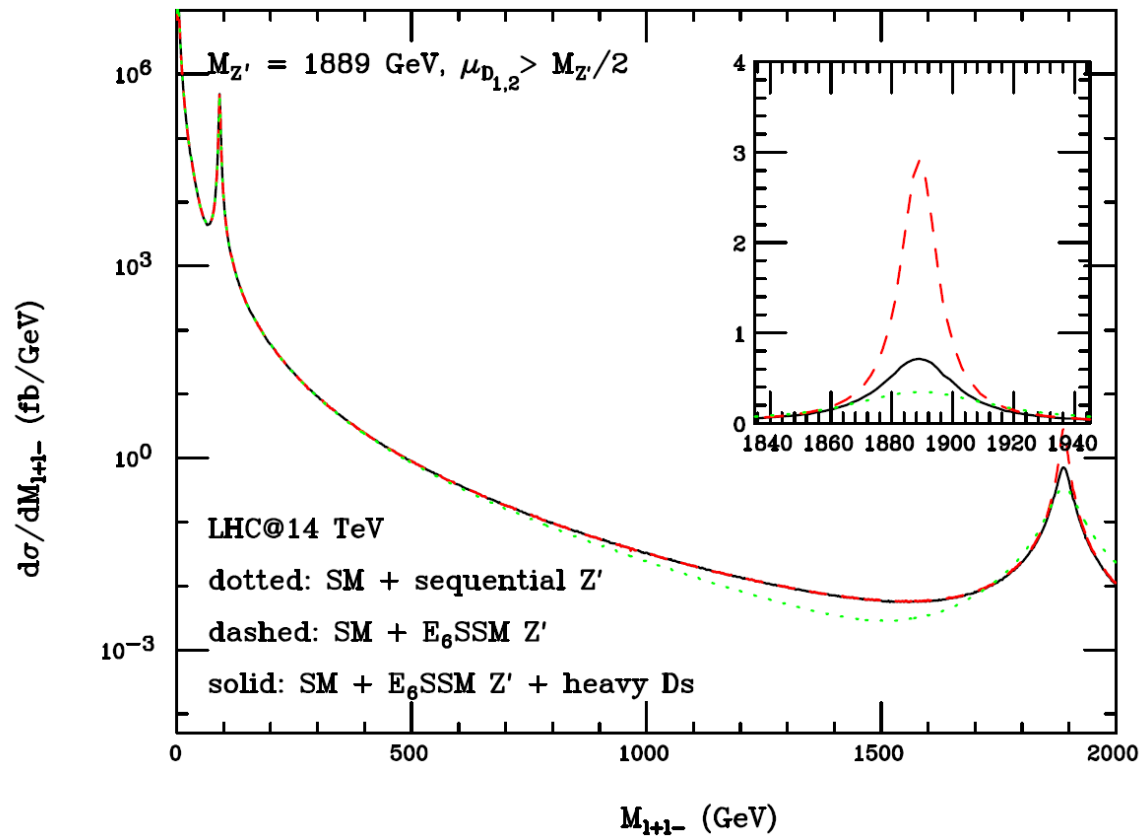
[Here we have set the singlino masses to 10 and 30 GeV]

## Benchmark C



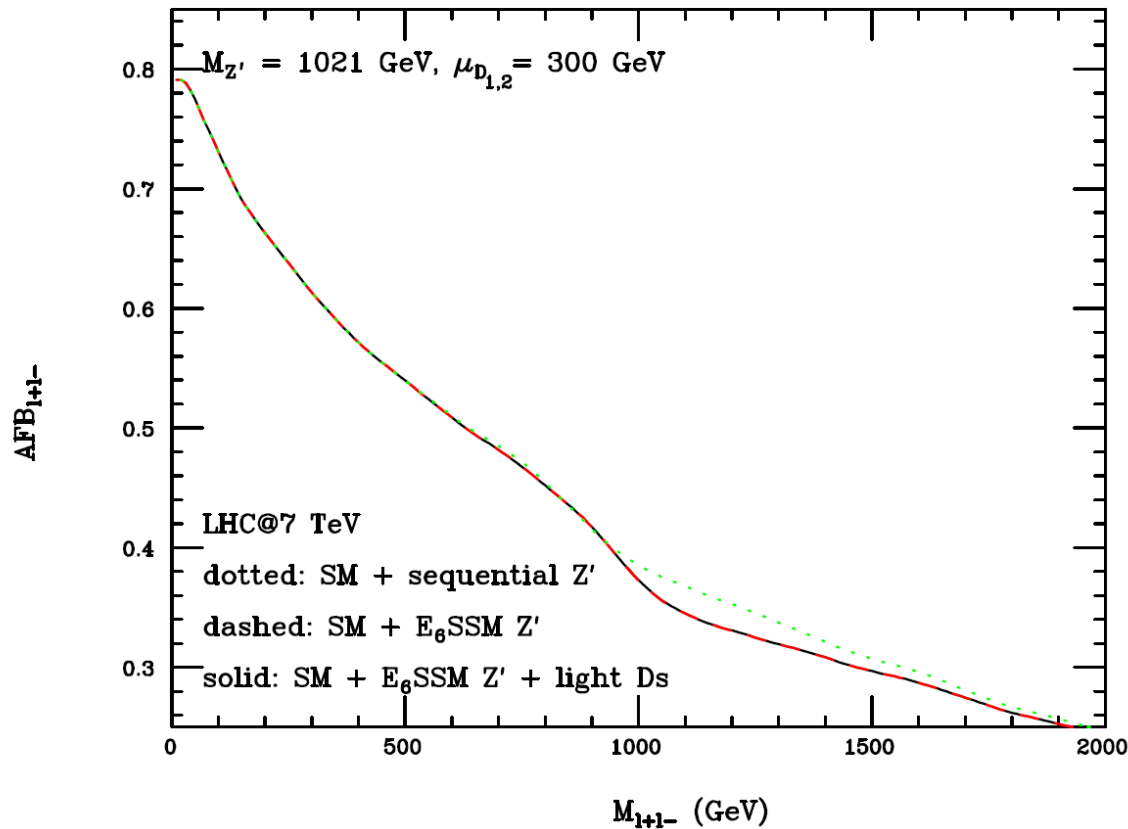
Z' width increases from  $\approx 7 \text{ GeV}$  to  $\approx 18 \text{ GeV}$  when exotic matter is included.

## Benchmark 4



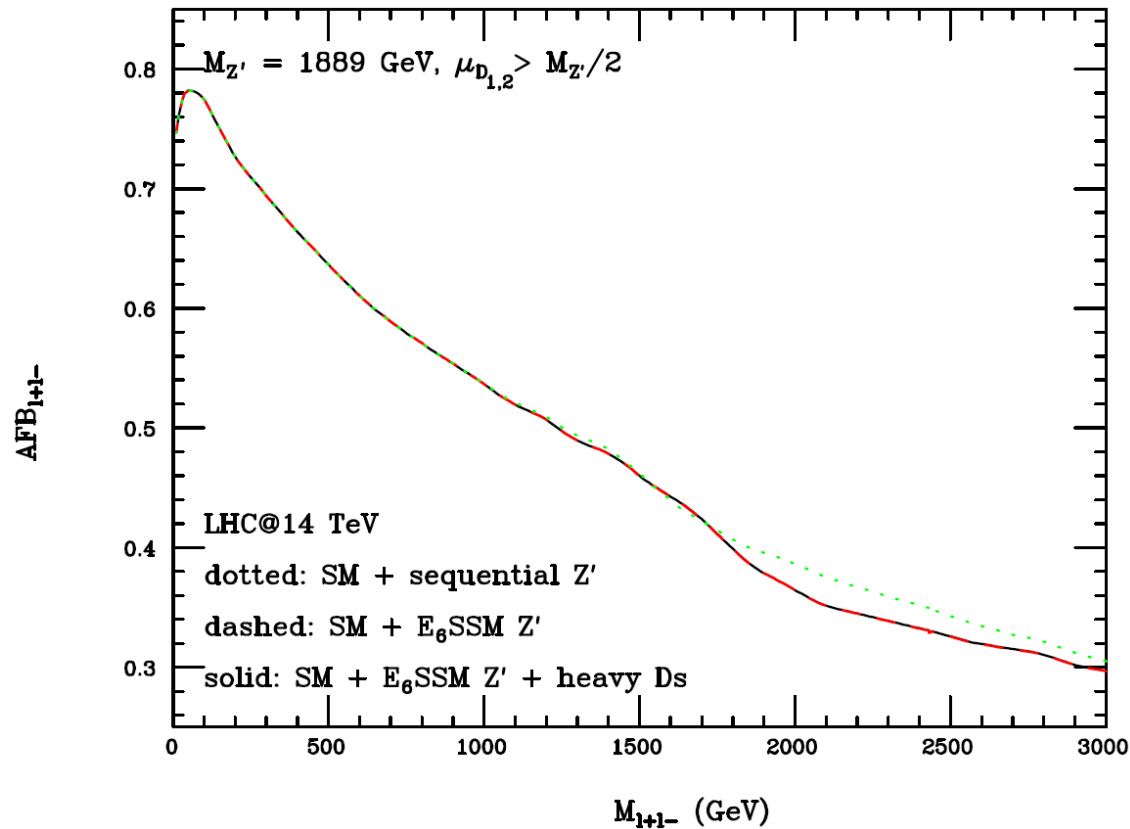
Note that this is now a  
14 TeV LHC.

## Benchmark C

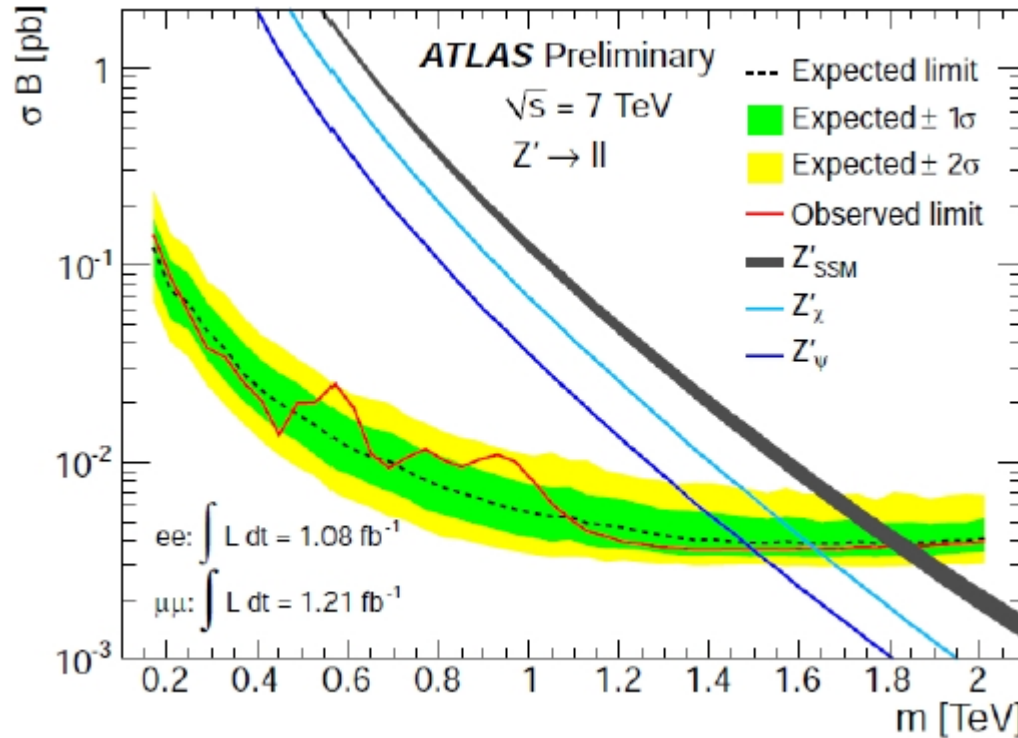


Notice that this is independent of the exotic content of the model.

## Benchmark 4



# LHC Z' exclusion limits



[Talk of Berger-Hryn'ova at EPS 2011]

LHC Z' limits are hard to interpret for the  $E_6$ SSM.

LHC limit  $M_{Z'_N} \gtrsim 1520$  GeV

(not shown on plot)

BMC has  $M_{Z'} = 1021$  GeV

BM4 has  $M_{Z'} = 1889$  GeV

**But** this isn't our  $Z'_N$  since it **does not include the exotic matter**.

We have already seen that  $Z'_N$  decays to exotic matter can substantially reduce the BR to leptons and weaken this limit.

BMC has  $BR_{l+l-} = 0.023$

BM4 has  $BR_{l+l-} = 0.028$

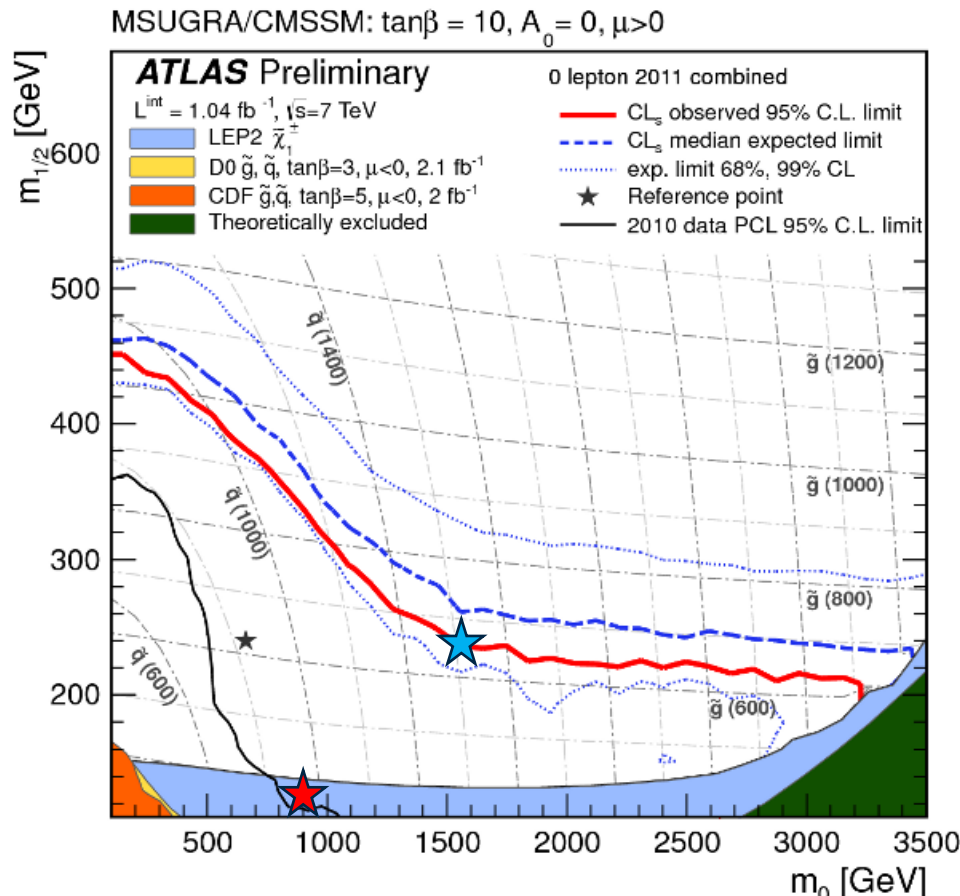
This can be compared to the Branching ratio if we neglect exotics:  $BR_{l+l-} = 0.055$  (both benchmarks)

Using the  $Z'_\psi$  line on the previous slide and estimating the effect of reducing the branching ratio we can estimate that the limit changes to  $\gtrsim 1300$  GeV

So **BMC is almost certainly ruled out** by this measurement, but BM4 is not.



# LHC Squark and Gluino Limits



[Talk of Dave Charlton at EPS 2011]

There has been no LHC analysis for squarks and gluinos in the  $E_6$ SSM but we can use cMSSM limits to try and gain some insight.

**BMC:**

$$m_{\tilde{q}_L} = 929 \text{ GeV}$$

$$m_{\tilde{g}} = 353 \text{ GeV}$$

**BM4:**

$$m_{\tilde{q}_L} = 1595 \text{ GeV}$$

$$m_{\tilde{g}} = 642 \text{ GeV}$$

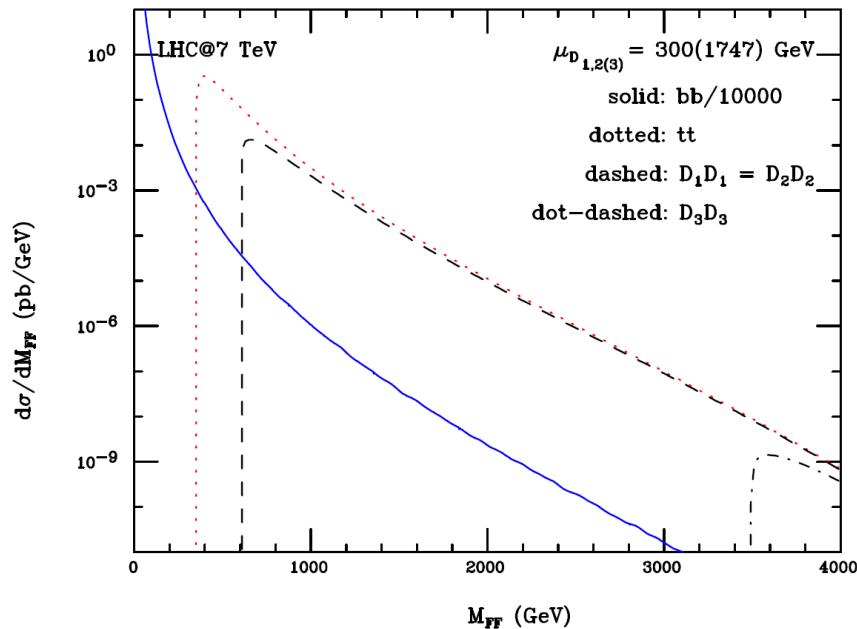
BMC looks ruled out while BM4 looks close to exclusion.

But remember that this is not an  $E_6$ SSM analysis (and uses different parameters), so it is too early to rule out BM4!

# Exotic D-fermion production

Since the exotic quarks are colored, their production cross-sections are very large

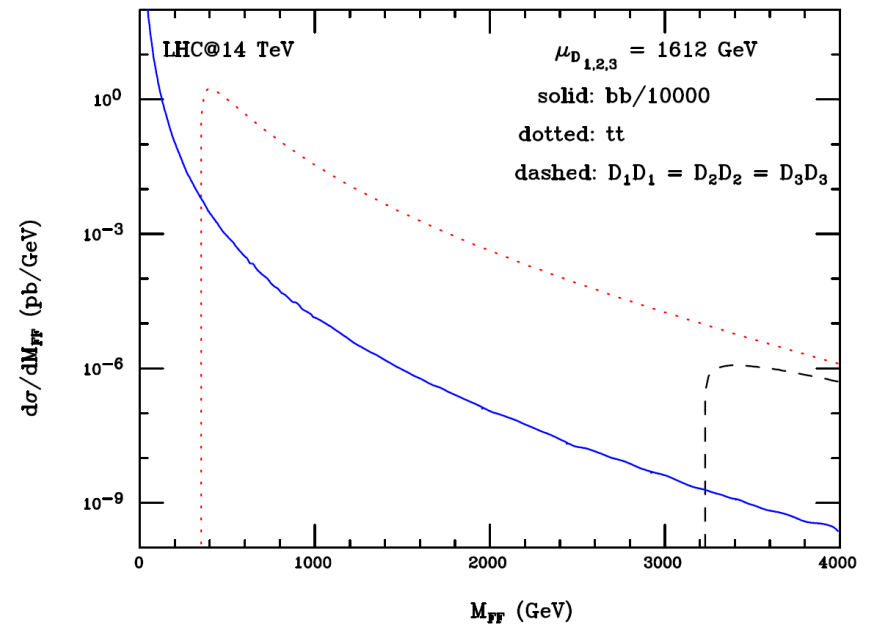
Benchmark C



$$\sigma(D_1D_1) = \sigma(D_2D_2) = 3 \text{ pb}$$

$$\sigma(D_3D_3) = 0.0005 \text{ fb}$$

Benchmark 4



$$\sigma(D_1D_1) = \sigma(D_2D_2) = \sigma(D_3D_3) = 0.9 \text{ fb}$$

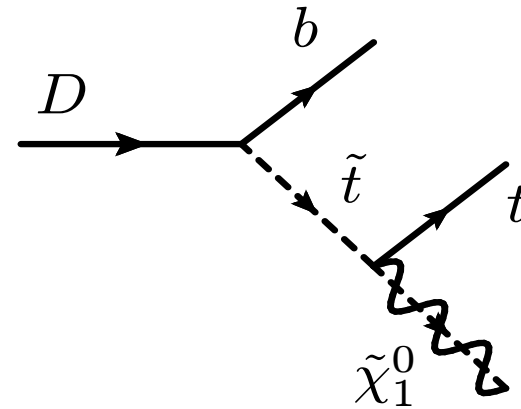
# Exotic D-fermion decays

Decays of the exotic D-fermions are facilitated by the  $Z_2^H$  violating operators (that we set to be small earlier), e.g.  $g_{ijk} D_i (Q_j Q_k)$

Assuming Ds couple predominantly to the 3<sup>rd</sup> generation:

Diquarks decay to  $\tilde{t}b$ ,  $t\tilde{b}$ , so would give an enhancement to

$$pp \rightarrow t\bar{t}b\bar{b} + E_T^{miss} + X$$



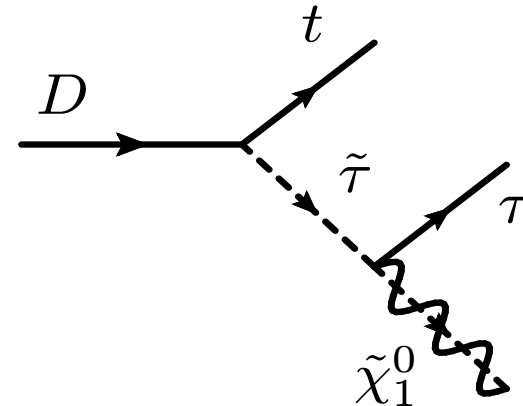
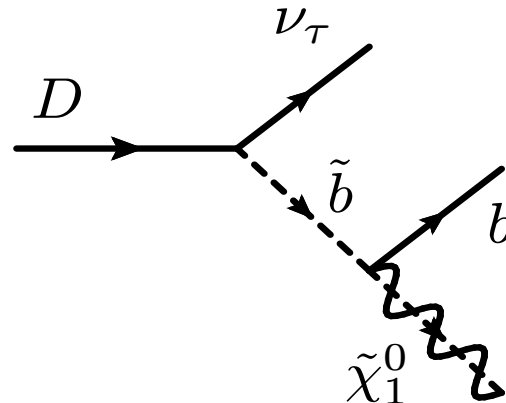
If the  $Z_2^H$  violating coupling is very small, D quarks may hadronize before they decay leading to spectacular signatures.

# Exotic D-fermion decays

Leptoquarks decay to  $\tilde{t}\tau$ ,  $t\tilde{\tau}$ ,  $\tilde{b}\nu_\tau$ ,  $b\tilde{\nu}_\tau$  so give enhancements to

$$pp \rightarrow t\bar{t}\tau^+\tau^- + E_T^{miss} + X$$

$$pp \rightarrow b\bar{b} + E_T^{miss} + X$$



Notice that SM production of  $t\bar{t}\tau^+\tau^-$  is suppressed by  $(\alpha_W/\pi)^2$  in comparison to  $t\bar{t}$

In BM4 the **exotic scalars**  $\tilde{D}$  are rather light (due to mixing):  $m_{\tilde{D}_{1,2}} = 312 \text{ GeV}$

Note that these are  $Z_2^{\text{B/L}}$  even, so don't need to decay to the LSP.

The Tevatron rules out the scalar diquarks lighter than about 630 GeV and scalar leptoquarks lighter than about 300 GeV, so these would need to be the leptoquarks.

Production cross-sections are  $\approx 0.53 \text{ pb}$  and  $\approx 4.9 \text{ pb}$  at a 7 TeV or 14 TeV LHC respectively.

They give an enhancement to, e.g.  $pp \rightarrow t\bar{t}\tau\bar{\tau} + X$

**Inert Higgs** decays are similar to their MSSM counterparts

$$H_{1,i}^0 \rightarrow b\bar{b} \quad H_{1,i}^- \rightarrow \tau\bar{\nu}_\tau$$

$$\tilde{H}_i^0 \rightarrow t\tilde{t}^* \quad \tilde{H}_i^0 \rightarrow \tau\tilde{\tau}^* \quad \tilde{H}_i^+ \rightarrow t\tilde{b}^* \quad \tilde{H}_i^- \rightarrow \tau\tilde{\nu}_\tau^*$$

- The  $E_6$ SSM provides an example of a model which could arise from a GUT, where each generation forms a complete 27-plet of  $E_6$ .
- We have examined a **constrained  $E_6$ SSM**, using RGEs to construct realistic benchmark scenarios at LHC energies.
- The model predicts a light gluino, much lighter than the squarks, new exotic quarks and squarks, “inert” Higgs bosons, and a  $Z'$ .
- Already LHC results have ruled out our “early discovery” benchmark with limits from  $Z'$  production and squark/gluino production, but other benchmarks are still very viable.
- If the new exotic quarks are light, they will give striking signatures, such as a significant enhancement to  $pp \rightarrow t\bar{t}b\bar{b} + E_T^{miss} + X$  which should soon be observable at the LHC.